



Article

Comparative Sensitivity of Vegetation Indices Measured via Proximal and Aerial Sensors for Assessing N Status and Predicting Grain Yield in Rice Cropping Systems

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Abstract: Reflectance-based vegetation indices can be valuable for assessing crop nitrogen (N) status and predicting grain yield. While proximal sensors have been widely studied in agriculture, there is increasing interest in utilizing aerial sensors. Given that few studies have compared aerial and proximal sensors, the objective of this study was to quantitatively compare the sensitivity of aerially sensed Normalized Difference Vegetation Index (NDVI) and Normalized Difference Red-Edge Index (NDRE) and proximally sensed NDVI for assessing total N uptake at panicle initiation (PI-N_{UP}) and predicting grain yield in rice. Nitrogen response trials were established over a 3-year period (10 site-years) at various locations throughout the Sacramento Valley rice growing region of California. At PI, a multispectral unmanned aircraft system (UAS) was used to measure NDVI_{UAS} and NDRE_{UAS} (average ground sampling distance: 3.7 cm pixel^{−1}), and a proximal GreenSeeker (GS) sensor was used to record NDVI_{GS}. To enable direct comparisons across the different indices on an equivalent numeric scale, each index was normalized by calculating the Sufficiency-Index (SI) relative to a non-N-limiting plot. Kernel density distributions indicated that NDVI_{UAS} had a narrower range of values that were poorly differentiated compared to NDVI_{GS} and NDRE_{UAS}. The critical PI-N_{UP} where yields did not increase with higher PI-N_{UP} averaged 109 kg N ha^{−1} (±4 kg N ha^{−1}). The relationship between SI and PI-N_{UP} for the NDVI_{UAS} saturated lower than this critical PI-N_{UP} (96 kg N ha^{−1}), whereas NDVI_{GS} and NDRE_{UAS} saturated at 111 and 130 kg N ha^{−1}, respectively. This indicates that NDVI_{UAS} was less suitable for making N management decisions at this crop stage than NDVI_{GS} and NDRE_{UAS}. Linear mixed effects models were developed to evaluate how well each SI measured at PI was able to predict grain yield. The NDVI_{UAS} was least sensitive to variation in yields as reflected by having the highest slope (2.4 Mg ha^{−1} per 0.1 SI). In contrast, the slopes for NDVI_{GS} and NDRE_{UAS} were 0.9 and 1.1 Mg ha^{−1} per 0.1 SI, respectively, indicating greater sensitivity to yields. Altogether, these results indicate that the ability of vegetation indices to inform crop management decisions depends on the index and the measurement platform used. Both NDVI_{GS} and NDRE_{UAS} produced measurements sensitive enough to inform N fertilizer management in this system, whereas NDVI_{UAS} was more limited.

Keywords: rice; nitrogen; precision management; grain yield; panicle initiation; canopy reflectance; Sufficiency-Index; NDVI; NDRE; UAS; GreenSeeker

1. Introduction

Remote sensing has emerged as a powerful technology to inform sustainable agro-nomic management by providing an accurate and timely assessment of the status of developing crops [1]. Agricultural remote sensing is based on the collection of crop canopy reflectance spectra at specific wavelengths in the electromagnetic spectrum, usually corresponding to regions where the canopy experiences strong absorption or reflectance of

incoming radiation [2]. A common method to interpret canopy reflectance data is to use the wavelengths to develop a vegetation index (VI), which is a mathematical combination of wavelengths related to specific biophysical characteristics of the plant [3]. Over the past decade, sensors have developed rapidly with higher spatial and spectral resolution. Similarly, better platforms are available that can carry such sensors and easily maneuver over large areas, which has led to a significant broadening of remote sensing applications in many fields including agriculture [4]. Some of the current applications of remotely sensed data in agriculture include biomass estimation, assessing crop nutritional status, detecting plant stress, identifying disease incidence, scouting for weeds, and predicting potential yield.

Some important applications of remote sensing in rice (*Oryza sativa* L.) are the assessment of crop nitrogen (N) status and prediction of grain yield. Nitrogen is an essential element for plant growth, and an adequate supply of N is fundamental to maximizing rice grain yield and quality [5]. However, overapplication of N fertilizer in rice and other crops has been associated with reduced yields and lodging [6], as well as harmful impacts on the environment through nitrate leaching [7], greenhouse gas emissions [8], or eutrophication of downstream aquifers [9]. The most accurate method to assess plant N status is by plant tissue analysis, but this technique is time consuming and lab results are often received past the time when decisions need to be made [10]. Alternative methods to assess N status in rice include using the Soil Plant Analysis Development (SPAD) chlorophyll meter [11] or the Leaf Color Chart [12]. While these tools are useful, they are limited by their single leaf sampling method, thus making it difficult to utilize these tools to accurately assess crop N status over large areas [10,13]. The development of remote sensing techniques provides a promising alternative to address this issue.

Remote sensing data can be collected using different platforms, including proximal handheld sensors or aerial sensors mounted to airplanes, satellites, or unmanned aerial vehicles (UAV; sensor mounted to a UAV is referred to as an unmanned aircraft system, UAS) [4]. Over the past two decades, most agricultural remote sensing research has focused on the use of proximal sensors, especially those that utilize an active light source [13]. However, with the recent expansion of compact aerial sensors that can be easily mounted to a UAV, an increasing number of studies have shifted toward utilizing UAS-based platforms [14]. Relative to proximal and UAS-based remote sensing, airplane and satellite-based measurements are less frequently used in agricultural applications due to the high complexity and costs of operating an airplane and insufficient spatial and temporal resolution often experienced with satellite imagery [15]. However, despite being more convenient than airplane and satellite-based remote sensing, both proximal and UAS-based remote sensing also come with their own unique advantages and disadvantages.

Among proximal sensors, the GreenSeeker (GS) HandHeld (Trimble Inc., Sunnyvale, CA, USA) has been one of the most commonly used in agricultural research. It is an active canopy sensor, which permits the collection of reflectance data at any time of day, regardless of ambient light conditions or cloud cover [13]. The GS measures canopy reflectance at specific bands in the red (670 nm) and near infrared (780 nm) spectral regions and displays the Normalized Difference Vegetation Index (NDVI), which is a useful measure of plant productivity and is among the most commonly measured indices in agricultural remote sensing applications [16,17]. Studies have tested the utility of GS NDVI ($NDVI_{GS}$) as an N management tool in rice systems and reported strong correlations between $NDVI_{GS}$ and aboveground biomass, total N uptake (N_{UP}), and grain yields [18–20]. Others have reported similar results for wheat (*Triticum aestivum*) [21] and maize (*Zea mays*) [22,23]. However, despite showing good utility in these crops, a key disadvantage of the GS is that it only measures NDVI, which loses sensitivity (i.e., saturates) once crop biomass exceeds a certain threshold [17].

When collecting canopy reflectance data aerially, typically a passive multispectral sensor is mounted to a UAV and flown in a grid-style pattern over the field or experimental area. This facilitates the assessment of larger areas and enables the identification of spatial

variability that is often present within a field [24–26]. An example of one such multispectral sensor frequently used in agricultural applications is the MicaSense Red-Edge M (MicaSense, Inc., Seattle, WA, USA). This is a passive sensor that collects canopy reflectance across five spectral bands (blue, green, red, red-edge, and near infrared) [27]. The additional bands included in multispectral sensors such as the MicaSense sensor, provide an important advantage over proximal sensors like the GS in that they permit the calculation of a range of indices, including red-edge-based indices, among which the Normalized Difference Red-Edge Index (NDRE) is the most common [28]. The NDRE is based on a similar calculation to the NDVI, but incorporates a red-edge band in place of red, which allows the NDRE to be more resistant to the saturation problem inherent with NDVI [29,30]. Additionally, data collected with aerial multispectral sensors permit the use of more complex non-index-based classification techniques, such as spectral mixture models, texture analysis, or machine learning algorithms [31–33], which can also be used in combination with VIs to improve crop N status assessments by reducing saturation [34,35]. However, aerial-based remote sensing also has its own limitations, including the narrow timeframe around solar noon during which data are best collected, the high cost of UAS platforms, and the technical issues that UAS platforms can experience mid-air, such as loss of power or an engine breakdown [36,37].

Among studies that only used aerial sensors to assess N status in rice, Dunn et al. (2016) [28] reported strong correlations between NDVI and NDRE and N_{UP} , but found that NDRE saturated less than NDVI. Wang et al. (2021) [34] reported stronger correlations between NDRE and Red-Edge Chlorophyll Index when estimating N-index (ratio of N concentration between fertilized and non-fertilized plants), relative to NDVI, and Zheng et al. (2019) [38] reported that Red-Edge Chlorophyll Index correlated better with rice aboveground biomass than NDVI. In similar experiments on other crops, Walsh et al. (2018) [39] found that the red-edge-based indices exhibited a higher correlation with wheat N concentration than red-based indices. Becker et al. (2020) [40] did not evaluate NDVI but reported a stronger correlation between NDRE and grain yield than Green Leaf Index and Blue Reflectance Index in maize.

Although numerous studies have demonstrated the ability of NDVI and NDRE to assess crop N status and predict yields using either a proximal sensor or an aerial sensor, few studies have directly compared proximal and aerial sensors side-by-side. Among the few studies that have, Zheng et al. (2018) [41] reported that proximal NDVI (measured using a passive hyperspectral sensor) was better correlated with rice N concentration than aerial NDVI. Sumner et al. (2021) [42] measured NDVI and NDRE in maize and found that proximal NDVI and aerial NDRE were both more sensitive to changes in N fertilizer rate than aerial NDVI. In wheat, Hassan et al. (2018) [43] and Duan et al. (2017) [44] both found proximal and aerial NDVI measurements to be well-correlated to each other across a wide range of growth stages, though Duan et al. (2017) [44] reported that aerial NDVI measurements were confined to a narrower range than proximal NDVI.

Given the interest and promise of canopy reflectance technology along with the lack of studies comparing platforms and sensors, the objective of this study was to compare the sensitivity of aeri ally sensed NDVI and NDRE to proximally sensed NDVI for assessing N status and predicting grain yield of rice at panicle initiation (PI) growth stage. Specifically, the level at which each index saturated relative to total N uptake at PI ($PI-N_{UP}$) was quantified and examined relative to important thresholds for fertilizer N management in this system. Additionally, the relative sensitivity of each index to predict grain yield at PI was quantified as the slope of the resulting linear relationship. This was accomplished through field studies over a 3-year period at 10 locations throughout the Sacramento Valley rice growing region of California (CA), USA.

2. Materials and Methods

2.1. Site Description

Ten replicated N response trials (nine on-farm; one on-station) were established during the 2017 to 2019 rice growing seasons (referred to by proximity to nearest town or station and study year) throughout the Sacramento Valley rice growing region of CA (Figure 1, Table 1). The on-station site was established at the CA Rice Experiment Station (RES) near Biggs. The Sacramento Valley has a Mediterranean climate characterized by warm and dry conditions during the growing season (May to October). The average air temperature and precipitation during the three years of this study were 23.2 °C and 5.9 mm, respectively [45]. Pre-season soil samples were collected from the plow layer (approximately 0–15 cm) after tillage and prior to fertilizer application at each site and analyzed for pH, particle size, organic carbon, and total N. The soil properties at each site were typical for rice soils in this region (Table 1).

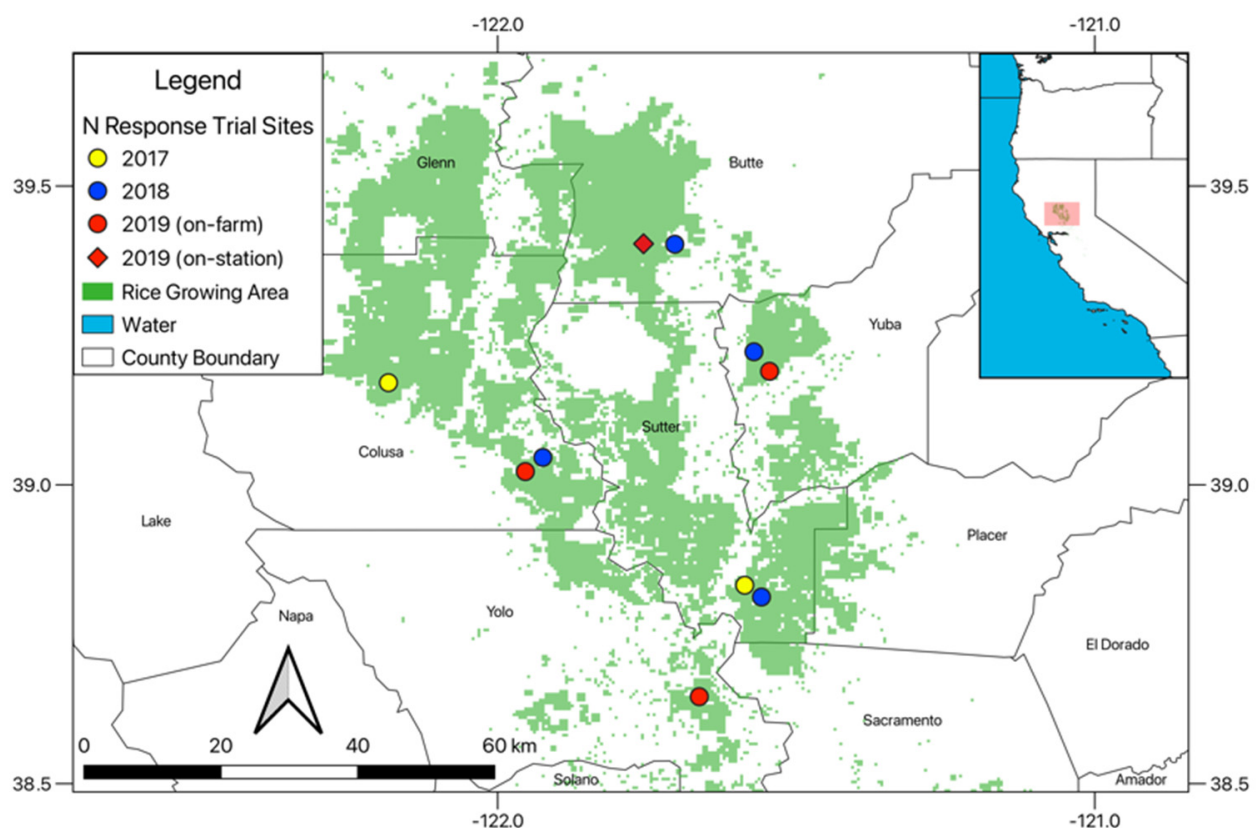


Figure 1. A map of N response trial sites established during the 2017 to 2019 growing seasons throughout the Sacramento Valley rice growing area of California, USA.

2.2. Experimental Design

Each N response trial was arranged as a randomized complete block design with four replicates. Treatments were pre-plant N fertilizer rates. In 2017, pre-plant N fertilizer was applied as urea at rates ranging from 0 to 225 kg N ha^{−1}, and in 2018 and 2019 pre-plant N fertilizer was applied as aqua-ammonia at rates ranging from 0 to 235 kg N ha^{−1}. Potassium (K) and phosphorus (P) fertilizers were broadcast across all plots at rates of 50 kg K₂O ha^{−1} as sulfate of potash and 45 kg P₂O₅ ha^{−1} as triple superphosphate to ensure these nutrients did not limit crop growth. The rice crop was established using water-seeding at all sites, which is the common practice in CA [46]. In this case, the fields are fertilized following seedbed preparation, flooded, and then soaked seed is broadcast onto the field by airplane. The medium grain rice variety M-206, which is commonly grown in CA, was planted at all sites. Herbicide and irrigation management followed common grower practice and was either managed by the growers (on-farm sites) or researchers (on-station site). The fields

remained continuously flooded until three weeks before harvest when they were drained to prepare for harvest.

Table 1. Soil descriptions and selected properties of each N response trial site-year located throughout the Sacramento Valley, California.

Site-Year	Soil Series	Taxonomic Classification	Texture (%)			Organic Carbon (%)	Total Nitrogen (%)	pH
			Sand	Silt	Clay			
Nicolaus-17	Capay	Fine, smectitic, thermic Typic Haploxererts	19	36	45	1.51	0.12	5.5
Williams-17	Willows	Fine, smectitic, thermic Sodic Endoaquerts	21	39	40	1.75	0.15	5.0
Arbuckle-18	Clear Lake	Fine, smectitic, thermic Xeric Endoaquerts	30	21	49	1.95	0.16	6.3
Biggs-18	Eastbiggs	Fine, mixed, active, thermic Abruptic Durixeralfs	50	30	20	1.60	0.12	4.9
Marysville-18	San Joaquin	Fine, mixed, active, thermic Abruptic Durixeralfs	39	39	22	1.64	0.13	4.6
Nicolaus-18	Capay	Fine, smectitic, thermic Typic Haploxererts	22	36	42	1.67	0.14	4.8
Arbuckle-19	Clear Lake	Fine, smectitic, thermic Xeric Endoaquerts	8	38	55	1.99	0.16	6.3
Davis-19	Sycamore	Fine-silty, mixed, super active, nonacid, thermic Mollic Endoaquerts	9	38	53	1.98	0.18	6.3
Marysville-19	San Joaquin	Fine, mixed, active, thermic Abruptic Durixeralfs	35	41	24	1.54	0.12	4.7
RES-19	Esquon-Neerdobe	Fine, smectitic, thermic Xeric Epiaquerts	30	26	44	1.38	0.11	5.3

2.3. Plant Sampling and Analysis

Biomass was collected at PI after canopy reflectance measurements (see below) by pulling all rice plants within a 0.5 m² quadrat from every plot. Within 24 h of collecting the samples, the biomass was washed to remove any residual soil, the roots were removed, and the aboveground shoots were oven dried to constant weight at 60 °C. Samples were then ground to pass a 4-mm sieve and ball-milled. Plant material was analyzed for total N using an elemental analyzer interfaced to a continuous flow isotope ratio mass spectrometer (EA-IRMS) [47]. From these samples, PI-N_{UP} was quantified as the product of aboveground biomass and N concentration. Rehman et al. (2019) [19] previously reported that NDVI_{GS} best assessed PI rice N status when quantified as PI-N_{UP}, rather than plant N concentration or aboveground biomass. Thus, PI-N_{UP} was selected as the N status parameter for the basis of comparison across the indices in this study.

Grain yield was determined at physiological maturity by harvesting all plants from a 1.0 m² quadrat. Grains were removed from panicles, cleaned using a seed blower, dried to constant moisture at 60 °C, and then weighed. Grain yields are reported at 14% moisture.

2.4. Measuring Canopy Reflectance

2.4.1. Sensors Used for Measuring NDVI and NDRE

The NDVI and NDRE were measured for each plot at PI using a proximal and/or aerial sensor (Table 2). The proximal sensor used in this study was the GreenSeeker (GS) handheld crop sensor (Trimble Inc., Sunnyvale, CA, USA). The GS is an active sensor and measures canopy reflectance at two specific spectral wavelengths (red and near infrared) and then automatically calculates and displays the NDVI. The GS NDVI (NDVI_{GS}) measurements were taken while walking steadily along the edges of each plot and holding the sensor in

the nadir position at a constant height of 1.0 m above the crop canopy and extended 90 cm from the edge of the plot. For each plot, the final NDVI_{GS} value represented the average of four NDVI_{GS} readings. Canopy closure was achieved by PI in all plots that received N fertilizer, thus the effect of background water or soil on canopy reflectance measurements was considered negligible in those plots.

Table 2. Summary of the proximal and aerial sensors used to measure the Normalized Difference Vegetative Index (NDVI) and the Normalized Difference Red Edge (NDRE) at the panicle initiation (PI) rice growth stage.

Vegetative Index	Sensor Type	Year	Sensor	Light Source	Spectral Band	Central Wavelength (nm)	Bandwidth [†] (nm)	Formula	Reference
NDVI	Proximal	2017–2019	GreenSeeker	Active	Red Near Infrared	670 780	10 10	$\frac{(Near\ IR - Red)}{(Near\ IR + Red)}$	[48]
	Aerial	2017	SlantRange 3P	Passive	Red Near Infrared	650 850	40 100		
		2018 & 2019	MicaSense RedEdge-M	Passive	Red Near Infrared	668 840	10 40		
		2017	SlantRange 3P	Passive	Red Edge Near Infrared	710 850	20 100		
NDRE	Aerial	2018 & 2019	MicaSense Red Edge-M	Passive	Red Edge Near Infrared	717 840	10 40	$\frac{(Near\ IR - Red\ Edge)}{(Near\ IR + Red\ Edge)}$	[49]

[†] full width at half maximum.

Two different aerial sensors were used in this study (Table 2). In 2017, canopy reflectance was measured using a SlantRange 3P (SlantRange Inc., San Diego, CA, USA) passive multispectral sensor. The autonomous flight mission was loaded onto the UAS using the DroneDeploy mobile app and images were captured at a height of 117 m above ground level (AGL) with 55% forward and side overlap. SlantView software (version 2.16.0) was used to process the multispectral imagery into a georeferenced orthomosaic with an average ground sampling distance of 4.8 cm pixel^{−1}. The SlantView software was also used to extract plot level canopy reflectance values for each of the spectral bands.

In 2018 and 2019, a MicaSense Red-Edge M (MicaSense Inc., Seattle, WA, USA) passive multispectral sensor was used to capture aerial imagery. The mobile app Pix4Dcapture was used to upload the flight mission onto the UAS, and images were captured at a height of 50 m AGL with 85% forward and side overlap. The software Pix4DMapper (version 4.2.27) was used to process the imagery into a georeferenced orthomosaic with an average ground sampling distance of 3.5 cm pixel^{−1}. Plot level reflectance values were extracted from the orthomosaic image using the recommended method of Haghighattalab et al. (2016) [50] as modified by Nelsen and Lundy (2021) [51].

All canopy reflectance measurements (proximal and aerial) occurred within 1 h of solar noon. In all years, the aerial sensor was mounted to a Matrice 100 UAV (DJI, Shenzhen, China). Before beginning each flight, images of a calibrated reflectance panel were taken to adjust for ambient light conditions. There was also an upwelling light sensor onboard the UAS that calibrated for incoming irradiance. Plot-level canopy reflectance values were converted into NDVI (NDVI_{UAS}) and NDRE (NDRE_{UAS}) using the formulas provided in Table 2.

2.4.2. Normalizing the Raw Vegetation Indices Using Sufficiency-Index

In order to directly compare the ability of each VI to quantify PI-N_{UP} and grain yield, the raw reflectance values from the three VIs were normalized by calculating the Sufficiency-Index (SI). The SI permits direct comparisons across VIs and measurement platforms on an equivalent numerical scale so that comparisons of statistical measures (e.g., range, slope)

are not confounded by inconsistent units among the VIs being compared. In addition, the SI produces a site-relative value such that VI values measured across multiple seasons with non-identical tools are normalized across the experiment. The SI is calculated by dividing the VI of the area of interest by the VI of an area where N was non-limiting (measured at the same location on the same day) [52]. The resulting SI values will typically range between 0 and 1, with higher values indicating a more N-sufficient crop and thus less likely to respond to additional N inputs [53–55]. In this experiment, the SI was calculated for each site by dividing the raw VI of each experimental unit by the mean VI of the experimental unit that received the highest pre-plant N application rate (using the mean VI of the highest N rate resulted in some experimental units to have a SI greater than 1.00) [56,57].

2.5. Data Analysis

Data analysis was performed using the statistical program R [58]. The degree of saturation for each index (raw VI and SI) was quantified using univariate kernel density distributions developed from the `geom_density()` function in the package `ggplot2` [59]. For all linear regression models developed in this study, graphical and numerical summaries were examined to ensure the resulting models satisfied the assumptions of linear regression. Simple linear (quadratic) regression models were developed to quantify the relationship between pre-plant N rate and both $PI-N_{UP}$ and grain yield at each site-year using the function `lm()` from the `stats` package [58].

Quadratic-plateau linear regression models were developed using the `nls()` function from the `stats` package [58] (following the method outlined by Mangiafico (2016) [60]) to quantify the relationships between: $PI-N_{UP}$ and each SI; $PI-N_{UP}$ and relative grain yield; pre-plant N rate and relative grain yield; and pre-plant N rate and each SI. For models that quantified the relationship between yield and $PI-N_{UP}$ and N rate, the effect of site-year was initially modeled as a random effect in a mixed, nonlinear model using the `nlme` package [61], but convergence was not achieved. Thus, site-normalization was accomplished by expressing absolute grain yield values relative to the site-year maximum and models were fit using `nls()`. For each of the quadratic-plateau models, the resulting model coefficients were used to identify the mean value and associated standard error range along the x-axis where each model reached a plateau. The function `nagelkerke()` from the `rcompanion` package [62] was used to calculate a pseudo coefficient of determination (R^2) for each quadratic-plateau model [63].

Linear mixed-effects regression models were developed to quantify the sensitivity of each SI for predicting grain yield using the function `lme()` in the `nlme` package [61]. The models contained a fixed-effect for SI and random-effects of site-year slope and intercept. The response variable was grain yield. A pseudo R^2 was calculated for each mixed-effects model using the function `r.squaredGLMM()` in the `MuMIn` package [64], with the conditional R^2 representing the variability explained by the entire model (fixed and random effects), the marginal R^2 representing the variability explained only by the fixed-effects, and the portion of variability explained by the random-effects represented as the difference in conditional and marginal R^2 .

3. Results

3.1. PI Total N Uptake and Grain Yield

At all sites, $PI-N_{UP}$ was lowest in the 0N treatment and ranged from 14 (Arbuckle-18) to 75 kg N ha^{−1} (Nicolaus-17) (Figure 2, left axis). At each site, $PI-N_{UP}$ increased with increasing pre-plant N rate. However, the magnitude of increase varied considerably across sites with maximum $PI-N_{UP}$ ranging from 94 (Davis-19) up to 209 kg N ha^{−1} (Nicolaus-17). In most cases, $PI-N_{UP}$ did not plateau with increasing N rate but continued to increase within the range of N rates used in this study.

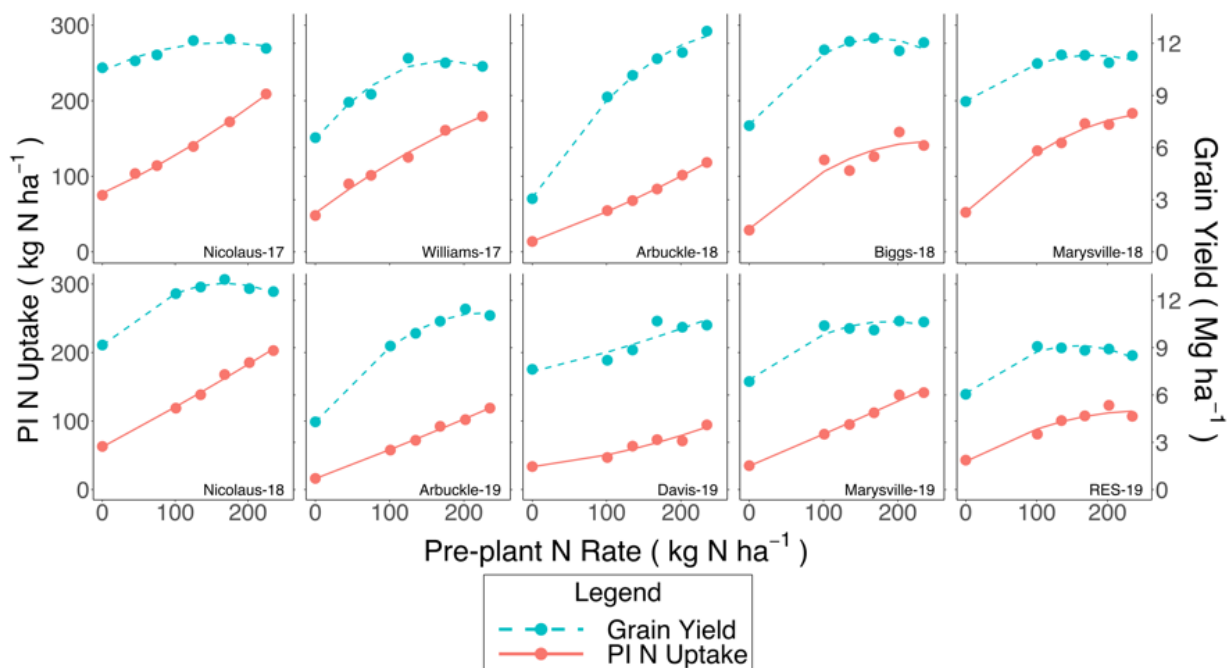


Figure 2. The relationship between pre-plant N rate and panicle initiation N uptake (PI-N_{UP}) (left axis) and grain yield (right axis) as described by quadratic linear regression models.

Similarly, at every site, grain yield was lowest in the 0N treatment, ranging from 3.1 (Arbuckle-18) up to 10.6 Mg ha^{-1} (Nicolaus-17) (Figure 2, right axis). Across all sites, yields increased with increasing pre-plant N rate up to a maximum and either plateaued or decreased at the highest N rates (with the exception of Arbuckle-18). Maximum yields ranged from 9.1 (RES-19) to 13.3 Mg ha^{-1} (Nicolaus-18). Based on the quadratic-plateau linear regression model, across sites maximum yields were achieved with an average pre-plant N rate of 183 kg N ha^{-1} ($\pm 18 \text{ kg N ha}^{-1}$) (Figure S1). Using a similar model, maximum yields were achieved across sites when PI-N_{UP} was $\geq 109 \text{ kg N ha}^{-1}$ ($\pm 4 \text{ kg N ha}^{-1}$) (Figure 3).

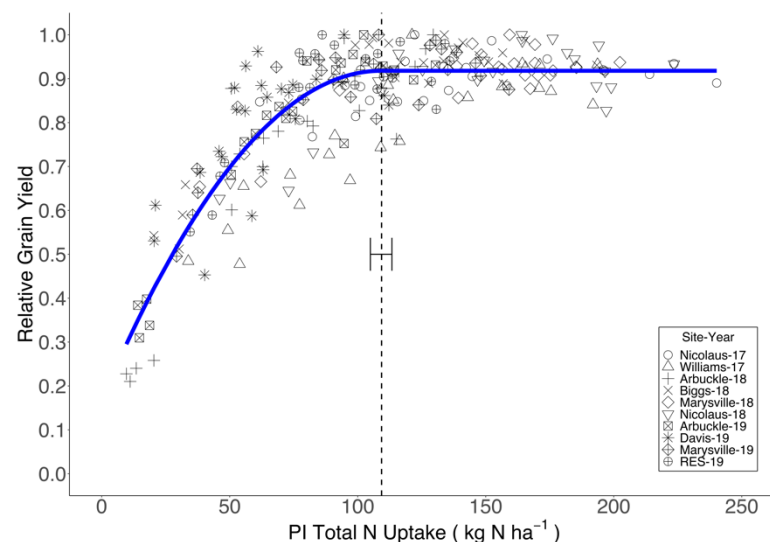


Figure 3. The relationship between total N uptake at panicle initiation rice growth stage (PI-N_{UP}) and relative grain yield as described by a quadratic-plateau linear regression model. The vertical dashed line at 109 kg N ha^{-1} represents the PI-N_{UP} value where the relationship reaches a plateau, and the error bar around the line represents the standard error.

3.2. Canopy Reflectance Data

There were differences in the kernel density distributions among the three indices in this study, both in terms of raw VI and SI (Figure 4). With respect to raw VI, NDVI_{UAS} exhibited the strongest saturation, as seen by the relatively high and narrow peak of NDVI_{UAS} VI observations centered around 0.90 (Figure 4a). The NDRE_{UAS} exhibited the least amount of saturation as the peak of NDRE_{UAS} VI values was lower and broader than the other two indices. The NDVI_{GS} was more saturated than NDRE_{UAS}, as seen by the higher and narrower peak of NDVI_{GS} VI observations. However, the NDVI_{GS} did detect lower values and was thus spread over a greater range than NDRE_{UAS}.

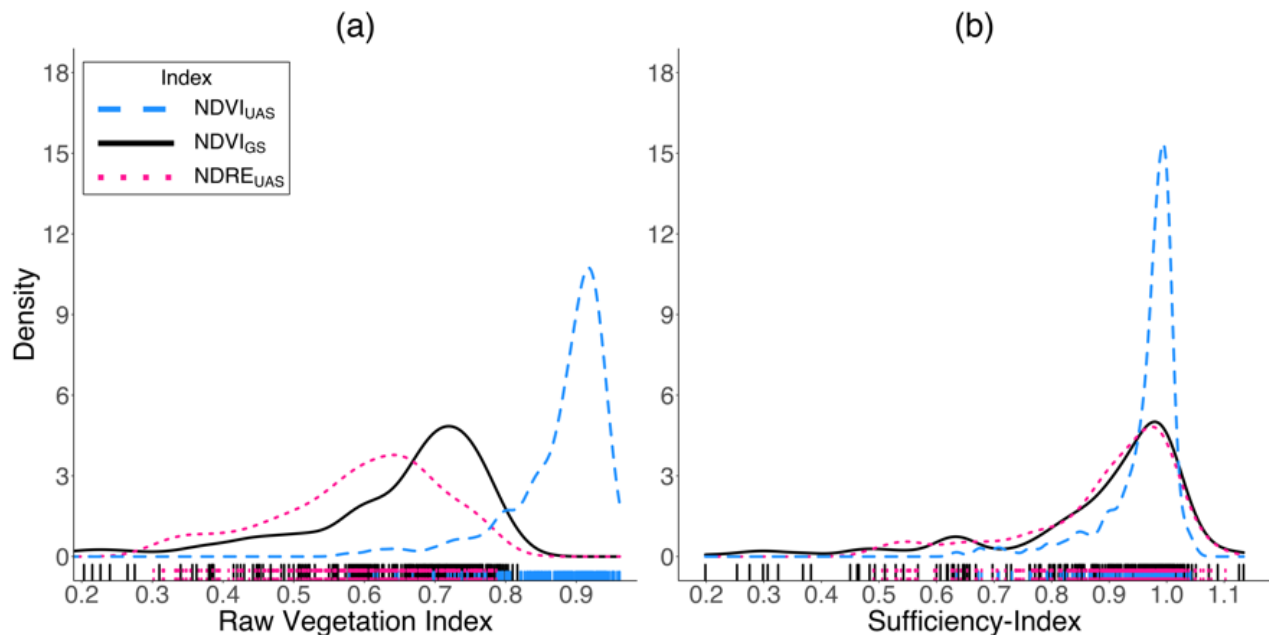


Figure 4. Kernel density distributions of unmanned aircraft system (UAS) Normalized Difference Vegetation Index (NDVI_{UAS}), GreenSeeker (GS) NDVI (NDVI_{GS}), and UAS Normalized Difference Red-Edge Index (NDRE_{UAS}) (a) raw vegetation index (VI) and (b) Sufficiency-Index (SI) measured at the panicle initiation (PI) rice growth stage.

Similarly, with respect to SI, the NDVI_{UAS} was the most saturated with 92% of the observations being ≥ 0.85 and having the narrowest range (0.63 to 1.04) (Figure 4b). The NDVI_{GS} had a larger range of SI observations (0.20 to 1.13) than NDRE_{UAS} (0.49 to 1.10); but both were similarly saturated as illustrated by the proportion of NDVI_{GS} (73%) and NDRE_{UAS} (74%) observations that were ≥ 0.85 .

3.3. Relationship between N Rate and PI-N_{UP} and Sufficiency-Index

To determine if the differences in saturation affected the ability of each index to accurately quantify the N status of the crop, quadratic-plateau linear regression models were developed to describe the relationship between PI-N_{UP} and each SI (Figure 5). In each case, SI increased with increasing PI-N_{UP} up to a threshold where it reached a plateau. The R^2 values (0.75 to 0.82) were similar for the different indices; however, the NDVI_{UAS} was the least sensitive to changes in PI-N_{UP}, as it plateaued (i.e., saturated) at the lowest PI-N_{UP} (96 kg N ha⁻¹) and had the narrowest range of observations along the y-axis (0.63 to 0.99) prior to its point of saturation (Figure 5c). In contrast, the NDVI_{GS} and NDRE_{UAS} were more sensitive to changes in PI-N_{UP} as illustrated by saturation at higher PI-N_{UP} values (111 and 130 kg N ha⁻¹, respectively). In addition, they had broader ranges of SI observations along the y-axis (0.20 to 0.97 and 0.49 to 0.97, respectively) prior to their respective points of saturation (Figure 5a,b). Similarly, quadratic-plateau linear regression models were developed to quantify the relationship between SI and pre-plant N rate and

determine at what pre-plant N rates the different indices saturated. Each SI increased with increasing pre-plant N rate until a plateau was reached (Figure 6). The NDVI_{UAS} saturated at the lowest N rate (166 ± 14 kg N ha⁻¹), followed by NDVI_{GS} (207 ± 14 kg N ha⁻¹) and NDRE_{UAS} (240 kg N ha⁻¹ \pm 15 kg N ha⁻¹).

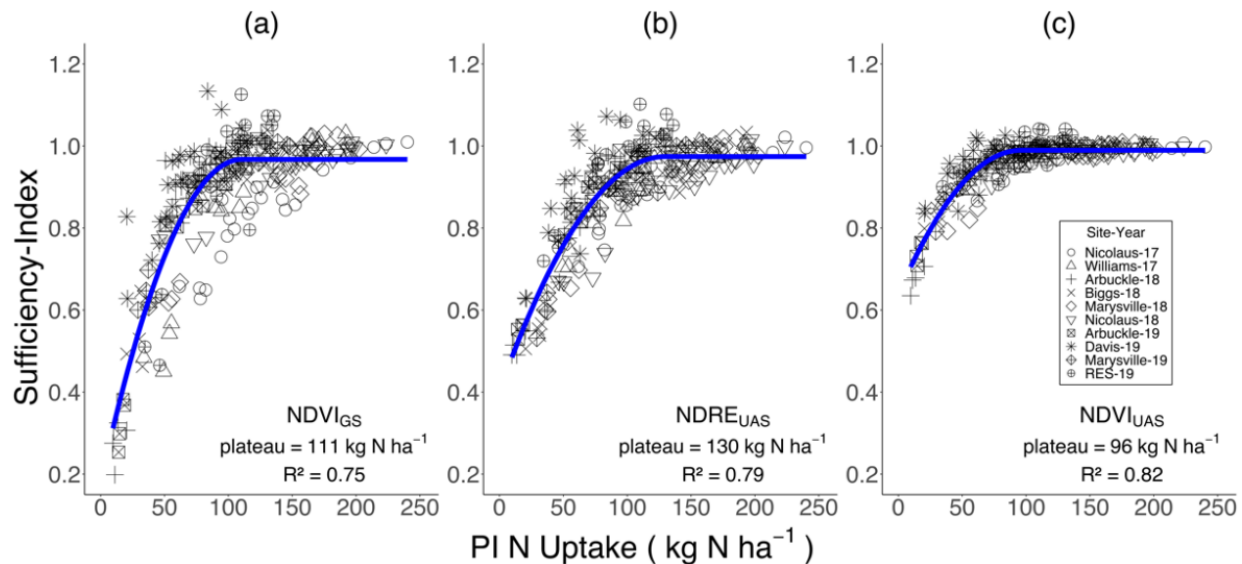


Figure 5. The relationship between panicle initiation N uptake (PI-N_{UP}) and (a) GreenSeeker (GS) Normalized Difference Vegetation Index (NDVI_{GS}) Sufficiency-Index (SI), (b) unmanned aircraft system (UAS) Normalized Difference Red-Edge Index (NDRE_{UAS}) SI, and (c) NDVI_{UAS} SI as described by quadratic-plateau linear regression models. The plateau value reported in each panel represents the PI-N_{UP} value where the regression model reached a plateau (i.e., the point of saturation for each index).

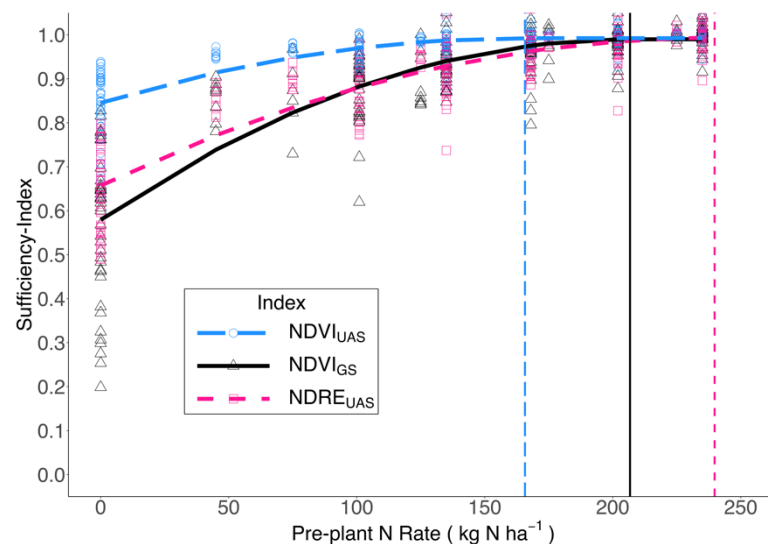


Figure 6. The relationship between pre-plant N rate and GreenSeeker (GS) Normalized Difference Vegetation Index (NDVI_{GS}) Sufficiency-Index (SI), unmanned aircraft system (UAS) Normalized Difference Red-Edge Index (NDRE_{UAS}) SI, and NDVI_{UAS} SI measured at panicle initiation (PI) rice growth stage as described by quadratic-plateau linear regression models. The vertical lines represent the N rate where the relationship for each SI reaches a plateau (i.e., the point of saturation for each index).

3.4. Relationship between SI Measured at PI and Grain Yield

The sensitivity of each SI for predicting grain yield was quantified using the slope of linear mixed-effects models where yield was the response variable and SI was the

independent variable. The greater (or steeper) the slope, the less sensitive the index is in determining grain yield. The slope of NDVI_{UAS} (2.4 Mg ha^{-1} per 0.1 SI) was more than double than that for NDVI_{GS} (0.9 Mg ha^{-1} per 0.1 SI) and NDRE_{UAS} (1.1 Mg ha^{-1} per 0.1 SI) (Figure 7). In addition, 87% of experimental units measured using NDVI_{UAS} had $\text{SI} \geq 0.90$ compared to 62% and 66% for NDRE_{UAS} and NDVI_{GS} , respectively. With many more undifferentiated SI observations, the variability around the yield outcomes for the NDVI_{UAS} observations was greater as well. Specifically, the standard deviation for site-relative grain yield was 10% for SI observations ≥ 0.90 measured via NDVI_{UAS} , compared to 6% and 7% for NDRE_{UAS} and NDVI_{GS} , respectively (data not shown). This indicates that for the same experimental unit, N status at PI was measured with greater sensitivity via NDRE_{UAS} and NDVI_{GS} than by NDVI_{UAS} , and therefore yield differentiation was less variable for the former two indices than for NDVI_{UAS} .

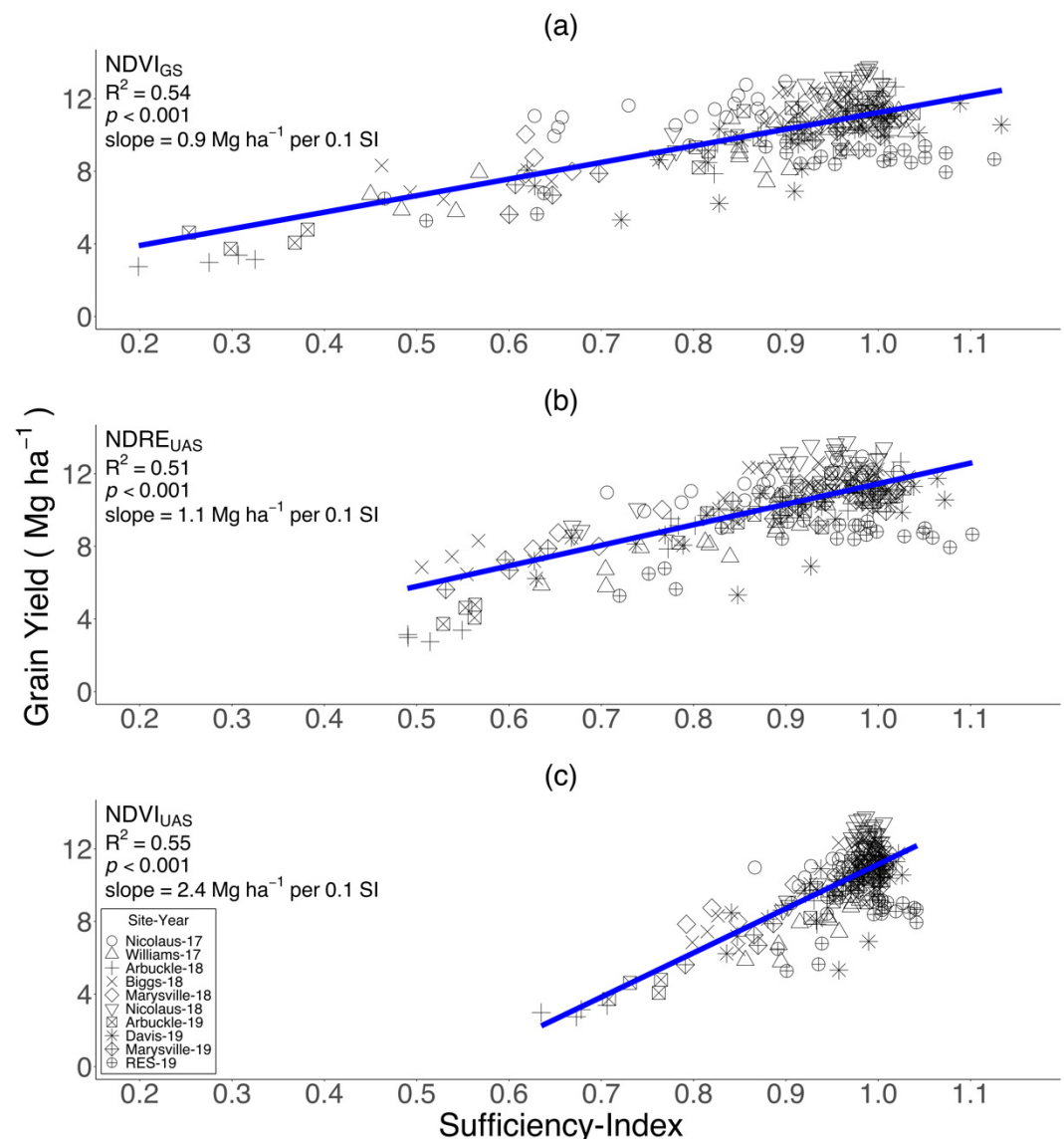


Figure 7. The relationship between (a) GreenSeeker Normalized Difference Vegetation Index (NDVI_{GS}) Sufficiency-Index (SI), (b) unmanned aircraft system (UAS) Normalized Difference Red-Edge Index (NDRE_{UAS}) SI, and (c) NDVI_{UAS} SI measured at panicle initiation (PI) rice growth stage and grain yield as described by linear mixed-effects models. The coefficient of determination (R^2) reported in each panel represents the proportion of variability explained by the model fixed effects only.

4. Discussion

4.1. Crop Response to N Fertilizer

Maximum grain yields ranged from 10.7 Mg ha⁻¹ to 13.3 Mg ha⁻¹ (Figure 2), which is within 75% of the maximum yield potential for this region [65], suggesting that the sites were not limited for other nutrients besides N and were not significantly affected by diseases or pests. The RES-19 site had lower maximum yields (9.1 Mg ha⁻¹), but this may be due to planting in June, which was later than the other sites and later than the typical planting time for rice in CA [46]. Grain yield plateaued in response to pre-plant N rate at all but one site (Arbuckle-18), which confirms that the highest N rate was not N limited and thus served as a valid non-N-limiting plot to calculate the SI.

The fertilizer N rate required to achieve maximum yields across sites ranged from 165 kg N ha⁻¹ up to 201 kg N ha⁻¹ and averaged 183 kg N ha⁻¹ (Figure S1), which is similar to the optimal N requirement reported by others for rice in CA [7,66].

Observed variability in N fertilizer response across sites in this study might be expected, given that trials were established over a 3-year period at varying locations with differing soils, management practices, and micro-climates. Similarly, there were large differences in the indigenous N supply of the soil as indicated by the wide range of PI-N_{UP} (14 to 75 kg N ha⁻¹) and yields (3.1 to 10.6 Mg ha⁻¹) in the 0N treatments across sites (Figure 2). Such variation in indigenous N supply across rice fields is common, yet it is difficult to predict and can have a large impact on optimal N fertilizer rates [67]. Across all sites, maximum PI-N_{UP} ranged from 94 kg N ha⁻¹ to 209 kg N ha⁻¹ (Figure 2, left axis). Unlike yields, PI-N_{UP} did not plateau at most sites, illustrating the ability of rice to take up large and even luxury amounts of N by PI as has also been shown by others [68]. The variability in indigenous N supply and N response seen in this study highlight the need to develop tools (such as canopy reflectance measurements) that can determine crop N status and help to optimize field- and year-specific N fertilizer management.

4.2. Index Saturation

Among the three indices evaluated in this study, NDVI_{UAS} exhibited the greatest degree of saturation, while the NDVI_{GS} and NDRE_{UAS} were less saturated (Figure 4). This was seen in both the raw VI (Figure 4a) and SI (Figure 4b) data. Saturation of red-based two-band indices, such as NDVI, is a well-documented problem [17,69], and a growing body of research has reported that red-edge-based indices, such as the NDRE, are less affected by saturation and can provide a better estimation of crop N status than NDVI, especially at higher levels of crop biomass [29,30,70]. Saturation of NDVI is attributed to the crop reaching 100% canopy cover but crop biomass beneath the canopy continuing to increase [17,71]. Once the crop reaches 100% canopy cover, near infrared reflectance continues to rise, but red reflectance remains relatively constant due to strong absorption by chlorophyll at the top of the canopy, thus resulting in a minimal change in the overall ratio (i.e., the denominator will have a greater impact on the ratio than the numerator) [19,72]. Red-edge radiation can penetrate deeper into the crop canopy due to relatively lower chlorophyll absorption, causing it to be more sensitive to chlorophyll content within the entire canopy, especially at higher biomass levels [29,73]. Given this greater sensitivity to total chlorophyll content within the canopy, red-edge-based indices are able to partially overcome the saturation problem inherent to NDVI [74,75].

A difference in saturation was also observed between the two NDVI-based indices, with the NDVI_{UAS} saturating more than NDVI_{GS} (Figure 4). Similarly, Duan et al. (2017) [44] reported from a wheat trial that NDVI_{UAS} was strongly correlated with NDVI_{GS}, but the NDVI_{UAS} readings were offset by about 0.2 units higher and were more compressed. A likely explanation for this difference could be that compared to the NDVI_{GS}, which is measured using an active sensor close to the canopy, the passive multispectral sensor used to measure NDVI_{UAS} cannot sample the small amount of background noise from a higher altitude due to lower spatial resolution, which results in a higher NDVI_{UAS} value with a smaller range [44].

Interestingly, $NDVI_{GS}$ and $NDRE_{UAS}$ both exhibited a similar degree of saturation (Figure 4). Given the lack of comparable studies, it is difficult to be certain what may be the explanation for this result. A possible explanation could be that despite being a red-based index, the closer proximity and active light of the $NDVI_{GS}$ allows it to overcome saturation to such a degree that it exhibits a similar level of saturation as the red-edge-based $NDRE_{UAS}$. It is also worth mentioning that $NDVI_{GS}$ had a larger range of observations than $NDRE_{UAS}$. Given this, it could be argued that $NDVI_{GS}$ is a more sensitive index. However, upon closer examination, the larger range of $NDVI_{GS}$ is attributable to relatively few observations that were measured in the unfertilized N treatment at a single site. The combination of the sparse stand at that site and the smaller sampling area of the $NDVI_{GS}$ compared to $NDRE_{UAS}$ may have magnified the noise-to-signal ratio in the $NDVI_{GS}$, which led to unusually low $NDVI_{GS}$ measurements [76]. Given that all other metrics of index sensitivity are functionally equivalent or favor $NDRE_{UAS}$, this difference in range should not be over-interpreted.

4.3. Practical Implications of Index Saturation

4.3.1. Approaches for Comparing Indices

A unique aspect of this study is the quantitative approach used to assess the sensitivity of the indices. For example, each VI was normalized by calculating the SI, which allows for the comparison across the different indices on an equivalent numeric scale [57]. Moreover, the sensitivity of each index was assessed with respect to where each SI saturated and was then related to relevant thresholds for N management within this system. This approach is in contrast to most previous agronomic studies in which the utility of an index is based on raw VI values and the R^2 of the regressions [39,77,78]. If such an approach were applied to this study, $NDVI_{UAS}$ would have been identified as the best index in the two cases examined, given its higher R^2 for PI- N_{UP} (Figure 5) and yield (Figure 7). However, when the point of saturation was quantified in relationship to where information was critical to making an informed management decision (i.e., for a mid-season N status assessment), the $NDVI_{UAS}$ performed the poorest. Similarly, the approach used for yield assessment quantified the sensitivity of the index to predict grain yield based on the slope of the relationship, and again the $NDVI_{UAS}$ was the least sensitive index. Therefore, more nuanced approaches are required when comparing across indices to understand the practical value of these tools to crop management.

4.3.2. Assessing Crop N Status and Predicting Grain Yield at PI

Assessing crop N status and predicting potential grain yield early in the season is of interest to farmers and agricultural stakeholders for a number of reasons, including refining N management, planning harvest, forecasting milling and storage needs, and directing marketing strategies. Refining N management requires an understanding of crop N status and the likelihood of the crop to respond to additional N inputs. In addition, this understanding must be gained early enough in the growing season so that subsequent N management decisions can still improve yields. Panicle initiation is an optimal and important stage for assessing N status and predicting grain yield in rice for several reasons. For example, PI marks the physiological shift from plant vegetative to reproductive growth [5], N applications later than PI are less efficiently utilized to affect yield outcomes [79], and in CA rice systems, most (if not all) pre-plant N fertilizer has been taken up by this stage [80,81]. Additionally, PI is an optimal time to collect canopy reflectance data, as measurements taken much earlier than PI can often experience a strong influence of background water and soil [76], while measurements taken after PI typically saturate or are obscured by panicle emergence causing interference in the spectral signal [18,82]. Importantly, while PI may be the best time with the sensors currently available, PI occurs roughly 45 to 55 days after planting, whereas the time to harvest is usually 130 to 150 days. This leaves almost two-thirds of the growing season in which multiple factors (biological, climate, etc.) can also impact the final yields. Thus, precision of sensor-based measurements taken at PI

will be higher under circumstances in which such factors do not limit crop growth post-PI. However, across 10 site-years, SI measurements taken at PI explained over half of the total variation in absolute grain yields (Figure 7) and more than two-thirds of the variation in site-relative yields (data not shown).

In terms of making midseason N management decisions, a key question is whether or not the indices saturate at a level that renders them useful. This was evaluated using two approaches. First, it was determined that, on average, a rice crop would respond to additional N fertilizer if $PI-N_{UP}$ was below 109 kg N ha^{-1} ($\pm 4 \text{ kg N ha}^{-1}$) (Figure 3). The $NDVI_{UAS}$ saturated at a $PI-N_{UP}$ of 96 kg N ha^{-1} (Figure 5) (below 109 kg N ha^{-1}), compared to the saturation points for $NDVI_{GS}$ and $NDRE_{UAS}$ at 111 and 130 kg N ha^{-1} , respectively. These data indicate that the $NDVI_{UAS}$ is the least useful for assessing midseason crop N status as it saturates at a level of $PI-N_{UP}$ that is less than the crop would need to ensure sufficiency and maximize yield on average. It also suggests that the $NDRE_{UAS}$ may be the most sensitive index given its relatively high saturation point with respect to $PI-N_{UP}$.

The second approach used to assess relative saturation of the indices and their practical value was to examine where each SI saturated based on the pre-season N rate applied. The recommended N management strategy for CA rice farmers is to apply the average seasonal N requirement before flooding and planting, and then assess crop N status at PI to determine if additional fertilizer N inputs are needed [6,66]. A similar recommendation is made for direct seeded rice systems in the Mid-South USA and Australia [83–86]. In CA, typical pre-plant N rates range from 150 to 200 kg N ha^{-1} , and data from this study generally support that range with N rates required for maximum yields ranging between 165 and 201 kg N ha^{-1} (Figure S1). The average pre-plant N rate at which $NDVI_{UAS}$ saturated was 166 kg N ha^{-1} , compared to 207 and 240 kg N ha^{-1} for $NDVI_{GS}$ and $NDRE_{UAS}$ SI, respectively (Figure 6). This suggests that for the pre-plant N rates typically used in this system, the $NDRE_{UAS}$ promises the most utility as it is sensitive across a much wider range of pre-plant N rates, including those that exceed the upper limit of the recommended range. In contrast, $NDVI_{UAS}$ appears to saturate before the relevant range of measurement. Importantly, both approaches used to determine index saturation and practical utility arrive at the same conclusion.

To our knowledge, this is the first study to evaluate the comparative ability of $NDVI_{GS}$, $NDVI_{UAS}$, and $NDRE_{UAS}$ for assessing crop N status or predicting grain yield in any major cereal crop. Previous studies comparing aerial and proximal sensors generally agree with the results presented here. For example, Zheng et al. (2018) [41] reported that proximal NDVI (measured with a hyperspectral sensor) was better correlated with rice N concentration than $NDVI_{UAS}$, a finding they attributed to less saturation of the proximal NDVI. In another study, Sumner et al. (2021) [42] reported that proximal NDVI (measured with a Yara N-Sensor) and $NDRE_{UAS}$ were more sensitive to changes in N fertilizer rate than $NDVI_{UAS}$ in maize. Among studies that only used aerial sensors to assess crop N status, the results of the current study agree with the findings of Dunn et al. (2016) [28], who also found that $NDVI_{UAS}$ and $NDRE_{UAS}$ both correlate well with rice $PI-N_{UP}$ but that $NDRE_{UAS}$ saturated less than $NDVI_{UAS}$ and provided a better basis for assessment.

In addition to the approaches mentioned above for N status assessment, the sensitivity of each index to predict grain yield at PI was quantified as the slope of the relationship between each SI and yield. The greater (or steeper) the slope, the less sensitive the index is in determining grain yield. As was the case when assessing N status, the $NDVI_{UAS}$ was also the least sensitive index for predicting yields, with SI values being confined to a narrower range of SI and thus having a higher slope (Figure 7). Both the $NDVI_{GS}$ and $NDRE_{UAS}$ were more sensitive to changes in yields and had a slope less than half of $NDVI_{UAS}$. These data indicate that $NDVI_{GS}$ and $NDRE_{UAS}$ have improved sensitivity for predicting grain yields over $NDVI_{UAS}$ at PI, which aligns with our findings regarding the relative sensitivity of each index for assessing crop N status. Although Zhou et al. (2017) [87] based their comparisons on R^2 , which is different from the approach used in the current study, the conclusions of both studies are similar, as they also found that $NDRE_{UAS}$ ($R^2 = 0.75$) was

better for predicting rice grain yield than NDVI_{UAS} ($R^2 = 0.66$) when compared at the booting stage (a few weeks after PI). Overall, the findings presented here can improve precision N management in this system by allowing farmers to utilize those indices that have suitable sensitivity for assessing crop N status and predicting yield at PI over those that lack the required sensitivity.

5. Conclusions

A unique approach was used to quantitatively assess the sensitivity of different VIs on a common numeric scale. Results indicated that both the NDRE_{UAS} and NDVI_{GS} measured rice crop N status and grain yield at PI with similar sensitivity. This is despite the fact that the former was measured using an aerial sensor at least 50 m above the crop while the latter was measured using an active proximal sensor within 1 m of the crop canopy. The ability to assess crop status effectively across different sensors provides a unique advantage for end-users as it allows flexibility to choose the sensor most suitable for their goals. In contrast, the NDVI_{UAS} had much less utility for the purposes examined in this paper. These findings should improve fertilizer management in these systems by identifying indices that serve as a better basis for the development of precision N management strategies. Given the relatively small number of studies that have explored this topic, additional studies are required to better understand how these results may be affected by the choice of rice variety, growth stage, biophysical parameter, or crop. Furthermore, with the rapid development of new sensors (both aerial and spaceborne) with higher spatial and spectral resolution, future research in this area should also explore how the findings presented here may be affected by the use of different platforms, sensors, or VIs.

Supplementary Materials: The following supporting information can be downloaded at: <https://www.mdpi.com/article/10.3390/rs14122770/s1>, Figure S1. The relationship between pre-plant N rate and relative rice grain yield as described by a quadratic-plateau linear regression model. The vertical dashed line at 183 kg N ha^{-1} represents the N rate where the relationship reaches a plateau, and the error bar around the line represents the standard error.

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